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The Structure of $C_9Cl_7(COOH).(O_2C_2H_4)$, a Condensed Cage Pentacyclononane Compound, Determined by the Symbolic Addition Method*

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The crystal structure of $C_9Cl_7(COOH).(O_2C_2H_4)$, a pentacyclononane derivative, was studied to obtain information on the configuration of the basic carbon cage structure which can be derived from a cube by adding one apex carbon atom. The crystal is monoclinic and the cell constants are: $a = 17.496 \pm 0.004$, $b = 8.005 \pm 0.003$, $c = 24.193 \pm 0.004$ Å, $\beta = 95.6 \pm 0.1°$; the space group is $I2/a$. Three-dimensional intensity data were collected on the CCXD, a computer-controlled diffractometer, which is operated by an IBM 1620 under a stored data-collection program. The crystal structure was determined by systematic application of the symbolic addition method and refined by a full-matrix least-squares program on an IBM 7094. The molecule can be called 6,6-ethylenedioxyheptachloropentacyclo-[5.2.0.0^{2,5}.0^{3,9}.0^{4,8}]nonane-3-carboxylic acid. The configurations of the cyclobutane and cyclopentane rings in the condensed cage molecule are discussed in detail. The carboxyl group is involved in the formation of centrosymmetric dimers which are stacked in the structure with the usual van der Waals contacts.

Introduction

Scherer, Lunt & Ungefug (1965) reported ring contraction through Favorskii rearrangement of chlorinated pentacyclodecanones by the action of alkali on I and III. In each case a pentacyclononane carboxylic acid has been formed (see Fig. 1). The position of the carboxyl group in IV could be uniquely assigned since the starting decanone possesses a symmetric cage structure; whereas for II the choice between the two non-equivalent sites for the group was decided by measuring the *pKa* value of the acid V obtained by a hydrolysis of II which effected a removal of the ethylene glycol residue.

Crystals of II and IV were studied as a part of our continuing effort to determine the shape and size of condensed poly-ring carbon cage structures. Although

IV is a simpler molecule than II, the crystallographic data revealed that there are two non-equivalent molecules per asymmetric unit. This led to determination of the crystal structure of II, which possesses an extra ethylenedioxy group on the apex carbon.

Experimental

Crystals of II, $C_9Cl_7(COOH)(O_2C_2H_4)$, were obtained from CH_2Cl_2 solution of the sample supplied by Professor K. Scherer. One such crystal was ground into an approximately spherical shape and mounted on a G. E. Goniostat on CCXD, a computer-controlled diffractometer system, operated by an IBM 1620 in a closed-loop manner (Cole, Okaya & Chambers, 1963). The crystallographic constants were measured on the diffractometer and used as input parameters to the subsequent data-collection program; the values were $a = 17.496 \pm 0.004$, $b = 8.005 \pm 0.003$, $c = 24.193 \pm 0.004$ Å,

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* The experimental part of this work was performed at IBM Research Center, Yorktown Heights, New York.

$\beta = 95 \cdot 6 \pm 0 \cdot 1°$. The apparent space group for this choice of axes was $I2/a$ or Ia. This unconventional choice of axes (resulting in a body-centered monoclinic cell) was employed to make the β angle close to 90°. A base-centered lattice may be obtained by a simple linear transformation of axes; e.g. $a = 17 \cdot 496 \pm 0 \cdot 004$, $b = 8 \cdot 005 \pm 0 \cdot 003$, $c = 28 \cdot 441 \pm 0 \cdot 004$ Å, $\beta = 122 \cdot 2 \pm 0 \cdot 1_0$, with space group $A2/a$ or Aa. There are eight formula units with observed density of $1 \cdot 809$ g.cm^{-3}, as compared to the calculated $1 \cdot 815$ g.cm^{-3}.

Three-dimensional intensity data were taken with Mo $K\alpha$. For each reflection the alignment of the specimen and the general accuracy of the system were tested first by optimizing the ω setting. The integrated intensity data were then recorded by making $(\theta - 2\theta)$ step scans; the number of steps was twenty-four. The intervals of the 2θ step scan varied according to the 2θ values; they are $0 \cdot 09°$ for 2θ less than 40° and $0 \cdot 11°$ thereafter. These intervals had been determined in such a way that the first three and the last three of the 24 steps represent the background at the 2θ value. In the course of optimizing the ω setting, the maximum and minimum counts were recorded; when the difference was smaller than the statistical fluctuation of the system, such a reflection was treated as unobserved. The data-collection program written in the 1620 SPS (Symbolic Programming System) language is explained elsewhere (Okaya, 1964).

Structure determination

The structure was solved by the symbolic addition method (Karle & Karle, 1963). An absolute scale factor and overall temperature factor were determined by a Wilson statistical analysis of the three-dimensional data and the normalized structure-factor magnitudes were then obtained. These were used in the phase determination by the direct method.

The ambiguity in the space group assignment was first resolved by a statistical analysis of the magnitudes of the E factors (Table 1), which shows beyond reasonable doubt the presence of a center of symmetry. The space group is thus determined as $I2/a$ (or $A2/a$ for the base centered transformed cell described above). The following set of equivalent positions for $I2/a$ was used in the analysis; (8); $(0,0,0)$ $(\frac{1}{2},\frac{1}{2},\frac{1}{2}) \pm (x,y,z; \frac{1}{2}+x,\frac{1}{2}-y,z)$.

Table 1. *Space group assignment by E factor statistics*

	Observed	Calculated for:* Centro	Non-centro
$\langle E^2 \rangle$	$1 \cdot 0$	$1 \cdot 0$	$1 \cdot 0$
$\langle |E| \rangle$	$0 \cdot 769$	$0 \cdot 798$	$0 \cdot 886$
$\langle E^2 - 1 \rangle$	$0 \cdot 974$	$0 \cdot 968$	$0 \cdot 736$
$|E| > 3 \cdot 0$	$0 \cdot 3\%$	$0 \cdot 3\%$	$0 \cdot 01\%$
$|E| > 2 \cdot 0$	$4 \cdot 8\%$	$5 \cdot 0\%$	$1 \cdot 8\%$

* Karle, Dragonette & Brenner (1965).

The phases of the larger E factors were systematically studied by the use of a program written in FORTRAN IV, *SORTE* (Bednowitz & Post, 1966), on an IBM 7094. After a number of iterative cycles, with application of the symbolic addition method, about 150 E factors were given with reasonably certain signs. These phases were then used in evaluating a three-dimensional E factor map, which was then scanned by a peak-searching program to obtain the positions of seven large peaks. Starting from these seven peaks the positions of other atoms were obtained by iterative structure-factor and electron density evaluations. After the sixteen remaining light atoms had been found in the electron density function, a view of the structure was drawn on an IBM 1627 XY-plotter based on a structure drawing program for an IBM 7094. The overall molecular shape of the compound is shown in Fig. 2.

The atomic coordinates were then refined by least-squares with anisotropic thermal parameters to represent the thermal vibration. After several cycles with a full matrix program, the error index, $R = \Sigma \, ||F_o| - |F_c||/\Sigma|F_o|$ was reduced to $0 \cdot 056$ (or $0 \cdot 068$ if all acciden-
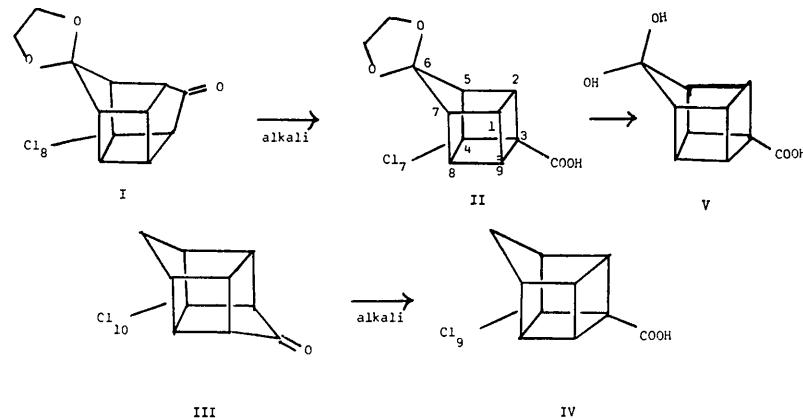
Fig. 1. Syntheses of the pentacyclononane acids studied in the present work. The numbering of atoms in the cage structure is given for molecule II.

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tally absent reflections were included as $F_{obs} \equiv 0$) for about 1800 reflections. The atomic coordinates, their standard deviations and anisotropic thermal parameters are shown in Table 2. The atomic scattering factors were those listed in *International Tables for X-ray Crystallography* (1962). The weighting scheme used in the least-squares refinement was: $\omega = 1 \cdot 0$ for $|F_{obs}| \leq 50 \cdot 0$ and $50 \cdot 0/|F_{obs}|$ for larger F values; the unobserved reflections were given weights of zero. Shifts of atomic coordinates at the last cycle of the refinement were negligible compared to their standard deviations. The positions of hydrogen atoms were not studied. Comparison between the observed and calculated structure factors is given in Table 3.

Discussion

The direct determination of the structure of the acid, II, led to the unambiguous solution of the configuration of the molecule. The molecule can be called 6,6-ethylenedioxyheptachloropentacyclo[$5.2.0.0^{2,5}.0^{3,9}.0^{4,8}$] - nonane-3-carboxylic acid. The observed position of the carboxyl group substantiates the earlier chemical evidence based on the acidity measurement. In Fig. 1, the numbering of atoms based on the pentacyclo system is shown. The basic cage structure has an approximate mirror plane going through carbon atoms 6,4,3, 9,7, a diagonal of this homocubane molecule, and this accounts for the inability to resolve the acid into optical isomers.

As shown in Fig. 3, this molecule belongs to a series of pentacyclo condensed cage compounds obtained by adding apex points to a cube. The configuration of the starting cube, cubane, C_8H_8 [Fig. 3(a)] has been studied

| ○ CARBON | ⊕ OXYGEN | ○ CHLORINE | HYDROGEN NOT SHOWN |
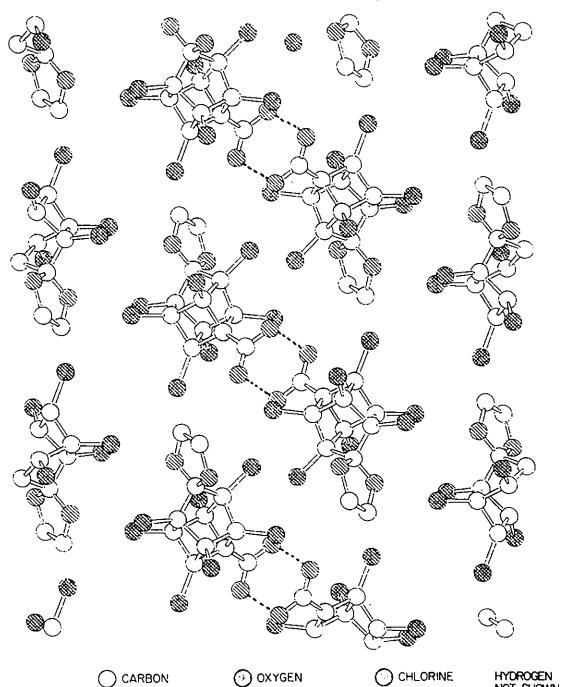
Fig. 2. Projection of the structure along the b axis. The O–H---O hydrogen bonds involved in the usual carboxyl dimer formation are shown by broken lines. The Figure was drawn on an IBM 1627 XY plotter based on a structure drawing program for the IBM 7094 (Okaya, 1968). The atomic coordinates and the peak heights, which were used in deciding proper shades for the atoms, are those obtained from electron density maps before the refinement stage.

(a) C_8H_8

Pentacyclo-[$4.2.0.0^{2,5}.0^{3,8}.0^{4,7}$]-octane

C_8H_8, cubane; Fleischer (1964).

(b) C_9H_{10}

Pentacyclo-[$5.2.0.0^{2,5}.0^{3,9}.0^{4,8}$]-nonane

$C_9Cl_7(O_2C_2H_4)(COOH)$;

This study.

(c) sym-$C_{10}H_{12}$

Pentacyclo-[$5.3.0.0^{2,6}.0^{3,9}.0^{4,8}$]-decane

$C_{10}Cl_{11}OSO_2Cl$; Okaya and Bednowitz (1967).

(d) gauche-$C_{10}H_{12}$

Pentacyclo-[$5.3.0.0^{2,6}.0^{3,10}.0^{4,8}$]-decane.
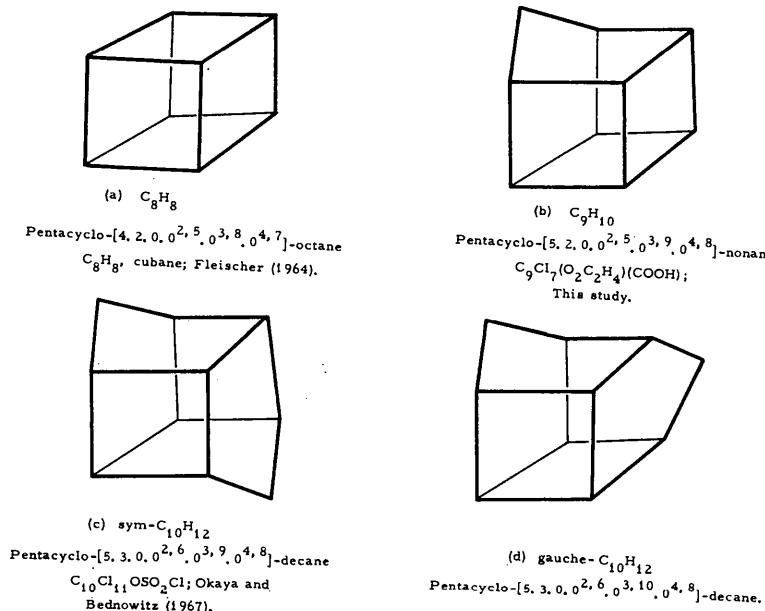
Fig. 3. The pentacyclo-cage systems discussed in the text.

by Fleischer (1964). The various crystallographic studies were made on symmetric decane derivatives, [Fig.3(c)]; e.g. the configuration of the cage was determined by a crystal structure analysis of its undecachlorochlorosulfonate derivative, $C_{10}Cl_{11}OSO_2Cl$ (Okaya & Bednowitz, 1967).

The bond distances are shown in Fig.4. It is obvious from the data that the formation of a condensed system has little effect on the bond distances; all the C–C and C–Cl bonds exhibit normal single-bond separations. By contrast, the bond angles and the configurations of the rings show more interesting features. Fig.6 lists the bond angles in the ring system and Fig.7 shows data on planarity of various groups in the cage. The two cyclobutane rings, 1–2–3–9, and 8–4–3–9, which have the apex carbon 6, only as a next nearest neighbor,

Table 2(a). *Atomic coordinates* (*in fractions of cell edges*) *and their standard deviations* (*in* 10^{-4} Å)

		x	y	z
Chlorine atoms	Cl(1)	0·14580 (24)	0·23967 (32)	0·23219 (24)
	Cl(2)	0·20534 (23)	0·43094 (24)	0·12481 (29)
	Cl(4)	0·10473 (22)	−0·04770 (25)	−0·00156 (23)
	Cl(5)	0·26656 (20)	0·15070 (26)	0·03736 (24)
	Cl(7)	0·16370 (24)	−0·17277 (31)	0·21669 (25)
	Cl(8)	0·04265 (21)	−0·23852 (24)	0·10524 (28)
	Cl(9)	−0·03155 (21)	0·12702 (27)	0·15871 (26)
Oxygen atoms				
Carboxyl	O(1)	0·08332 (52)	0·37560 (62)	0·00538 (60)
	O(2)	−0·01518 (46)	0·39473 (58)	0·05737 (53)
Ethylenedioxy	O(3)	0·25272 (48)	−0·18603 (56)	0·10761 (55)
	O(4)	0·29916 (49)	0·02115 (60)	0·16384 (56)
Carbon atoms				
	C(1)	0·13645 (76)	0·14458 (79)	0·16792 (78)
	C(2)	0·16586 (68)	0·23558 (83)	0·11676 (85)
	C(3)	0·08539 (67)	0·20320 (82)	0·08331 (77)
	C(4)	0·12228 (70)	0·03731 (79)	0·06418 (76)
	C(5)	0·20521 (70)	0·09472 (81)	0·08584 (76)
	C(6)	0·23479 (70)	−0·03389 (82)	0·12992 (79)
	C(7)	0·16233 (78)	−0·03740 (90)	0·16007 (81)
	C(8)	0·09283 (69)	−0·05300 (81)	0·11514 (83)
	C(9)	0·05655 (72)	0·11093 (78)	0·13372 (76)
	C carb	0·04622 (63)	0·33378 (79)	0·04571 (77)
	C ethy(1)	0·33294 (76)	−0·22833 (82)	0·12270 (109)
	C ethy(2)	0·36530 (74)	−0·07662 (86)	0·15315 (101)

Table 2(b). *Anisotropic temperature factors used in the expression*

$$\exp\left[-\{\beta_{11}h^2+\beta_{22}k^2+\beta_{33}l^2+\beta_{12}hk+\beta_{13}hl+\beta_{23}kl\}\right].$$

		β_{11}	β_{22}	β_{33}	β_{12}	β_{13}	β_{23}
Chlorine atoms							
	Cl(1)	0·00541	0·03744	0·00180	0·00307	−0·00013	−0·00587
	Cl(2)	0·00470	0·01449	0·00417	−0·00390	−0·00039	−0·00371
	Cl(4)	0·00419	0·02269	0·00179	0·00329	−0·00066	−0·00404
	Cl(5)	0·00345	0·02416	0·00249	0·00048	0·00183	0·00351
	Cl(7)	0·00511	0·03483	0·00234	0·00589	0·00066	0·00979
	Cl(8)	0·00353	0·01450	0·00394	−0·00259	0·00006	0·00209
	Cl(9)	0·00313	0·02730	0·00291	0·00366	0·00225	0·00175
Oxygen atoms							
Carboxyl	O(1)	0·00434	0·02334	0·00275	0·00623	0·00292	0·00520
	O(2)	0·00307	0·02049	0·00206	0·00567	0·00059	0·00064
Ethylenedioxy	O(3)	0·00367	0·01528	0·00236	0·00310	−0·00061	−0·00118
	O(4)	0·00337	0·02161	0·00237	0·00080	−0·00171	−0·00321
Carbon atoms							
	C(1)	0·00332	0·02114	0·00144	0·00186	0·00059	−0·00246
	C(2)	0·00221	0·01414	0·00214	−0·00182	0·00001	−0·00156
	C(3)	0·00213	0·01241	0·00168	0·00160	0·00063	−0·00022
	C(4)	0·00254	0·01480	0·00117	0·00137	0·00047	0·00074
	C(5)	0·00256	0·01512	0·00139	0·00084	0·00106	0·00099
	C(6)	0·00234	0·01284	0·00197	0·00009	0·00034	0·00036
	C(7)	0·00321	0·01583	0·00170	0·00120	0·00029	0·00338
	C(8)	0·00213	0·01421	0·00206	−0·00084	−0·00084	0·00150
	C(9)	0·00302	0·01724	0·00138	0·00149	0·00096	0·00013
	C carb	0·00165	0·01380	0·00190	0·00093	−0·00029	−0·00278
	C ethy(1)	0·00237	0·02452	0·00402	0·00518	−0·00037	−0·00200
	C ethy(2)	0·00223	0·02295	0·00338	0·00518	−0·00097	−0·00167

THE STRUCTURE OF $C_9Cl_7(COOH).(O_2C_2H_4)$

Table 3. *Comparison of observed and calculated structure factors* $(\times 10)$

```
 FO  FC          FO  FC          FO  FC          FO  FC          FO  FC          FO  FC          FO  FC          FO  FC          FO  FC
H,K= 0, 0     H,K= 1, 3     H,K= 2, 7     H,K= 4, 3     H,K= 5, 3     H,K= 7, 0     H,K= 10, 0    H,K= 12, 4    H,K= -2, 0    H,K= -3, 4
L=2 697 658   16 225 195    L=1  0  9     7 406 399     16 569 549    5  90 132     6 718 704     6 519 503     7 157 147
  412981217    18  69  29    3  95 110    9 471 475     18 239 164    7   0  39     8 322 344     815141645    9 594 581
  6 358 326    20  55  80    5 214 200    11 164 169    20   0  73               12 120 139      10 759 794    11 523 525
  814351381                  7 317 318    13   0  30                 H,K= 8, 0    13 280 280     12 399 416    13 494 511
 10  53  68   H,K= 1, 4                   15 295 291    H,K= 6, 1    L=0  62  64   12 221 242     14 381 404    15 243 236
 12   0  14   L=1 447 457   H,K= 3, 1     17 141 119    L=1 372 374  2 454 429    14 407 423     16   0  23    17 157 141
 14 184 170    3 172 184    L=0 113  96   19  72  27    3 453 440    4 768 745    16 315 367    H,K= 13, 1
 16 127 143    5 173 177    2 482 428                   5 274 267    6 720 704                   L=0 161 169   H,K= -3, 5
 18 746 749    7 475 478    4 929 896    H,K= 4, 4     7 275 288    8 147 172    H,K= 10, 1     2 349 356    L=2 108  83
 20   0  12    9  90  75    6 966 987    L=0 596 592    9 161 147    10 565 586   L=1 358 379    4 360 359     4   0  41
 22 145 134    11 232 191   8 734 738     2 588 573    11 179 121   12  99 107    3 298 282      6   0  54     6  53  37
               13  99 102   10 266 263    4 163 156    13 101  68   14 223 219    5   0  15     8 189 175    L=1 152 125
H,K= 0, 1      15   0  2    12   0  50    6 269 257    15 216 210   16 349 394    7 560 565     10 223 270     3  97 182
L=1 530 592   17 280 242    14   0  73    8 180 185    17   0  74   18 172 201    9 207 204                    5  49  68
 3 246 276                  16  92 118    10 493 482   19  44  89               11 147 171    H,K= 13, 2     7 237 246
 5 737 690   H,K= 1, 5     18 308 311    12   0  56                H,K= 8, 1    13 125 137    L=1 294 261     9 214 192
 7 957 974   L=0 230 221   20   0  78     14 164 165   H,K= 6, 2    L=1  0  0    15 115  89     3 115 109    11 218 202
 9 819 811    2 322 283                  16  62  84   L=0 487 483   3 212 218                   5 198 194    13 445 455
 11 879 832   4 221 275   H,K= 3, 2      18  46  76    2 405 407   5 596 614    H,K= 10, 2     7 290 271    15 301 310   L=1  81 118
 13   0  61   6  60  39   L=1 149 139                  4  53  79   7 230 231    L=010691077     9 218 237    17 228 260    3   0  21
 15  72  60   8  26  80    311931163    H,K= 4, 5     5  88 105   9  44  18     2   0  59                    19 478 476    5  58  74
 17  47  56   10   0  15    514791393   L=1 745 738   8 487 490   11 313 299    4 113 126     H,K= 13, 3    21   0  32     7 164 156
 19   0  53   12   0   0    7 319 314     3 115 123   10 636 624   13   0  69    6 280 279    L=0 198 210                   9   0   7
 21 258 246   14 133 131    9 447 420     5 203 208   12 363 348   15  85  76    8 431 447     2   0  53    H,K= -2, 2    11 127 129
              16 138 138    10  0  49     7  39  68   14 223 254   17  70  86    10 255 271     4  83  96    L=2 209 220
H,K= 0, 2                  13 308 309     9 743 727   16 234 242                 12   0   5     6 292 309     412381278   H,K= -3, 7
L=0 374 386   H,K= 2, 0    15 411 422    11   0  88   18 326 306   H,K= 8, 2    14   0  55                   6 526 515    L=2 250 244
 2 665 683   L=1 491 487   17 118  94    13 193 194               L=0  99 111               H,K= 13, 3    8 423 440     4   3  47
 4 179 228    3  56  18    19 129 145    15   0  40   H,K= 6, 3    2 892 900    H,K= 10, 3    L=1 122 142    10 264 272    6   0  79
  614041388   5 416 400    21 172 169                 L=1 333 331  4 131 140    L=1 282 270    2   0  53    12  83  47
  8  35  39   7 154 157                  H,K= 4, 6     3 234 231   6   0  57     2   0  53     4 459 470    14 299 318   H,K= -4, 0
 10 301 272   9 274 249   H,K= 3, 3      L=0   0  79   5 558 551   8 427 431    3 337 351     6  53  95    16 152 165   L=2 635 616
 12 475 446   11   0  37   L=0 152 133    2   0   0    7 131 131  10 713 712    5 260 255     8   0  48     18   0  67    4 260 281
 14 448 432   13 179 161   2 698 677     4  53  59    9 619 624   12   0   8    7   0  23                   20   0  57    6 392 381
 16 464 438                4 172 144     6   0  60   11   3  47   14   0  50    9 278 289     H,K= 14, 1                  8 205 223
 18   0   1   H,K= 2, 1    6 494 528     8 117 114   13 200 215   16   0  58   11 124 140     3   0  37    H,K= -2, 4   10 743 737
 20   0  83   L=0  88  95   8 294 289    10 101  68   15   0  14   18   0  56   13 189 181     5 124 150    L=1 305 322   12   0  50
              2 203 224   10 127 117    12   0  74   17 248 254                               7 292 281    3 159 156   14 894 916
H,K= 0, 3     4  83  62   12 290 268                              H,K= 9, 0    H,K= 10, 4                    5 379 417   16 289 291
L=1 526 543   6   0  67   14 147 163    H,K= 4, 7    H,K= 6, 4    L=1 319 306   L=0   0  69   H,K= 14, 2    7  30  66   18 409 381
  312471262             16 143 116     L=1 202 190   L=0 196 195  3 228 218    2 219 198     L=0  95  68    9 290 291   20   0  76
 5 393 402   H,K= 2, 2   18 273 248     3 285 278    2 179 160   5 337 337    4   0  27      2   0  98    11 342 324
 7  97 110   L=0 668 661   20  74  74    5   0  46    4   0  59   7 337 323    6 234 215     4 376 353    13 381 384   H,K= -4, 1
 9   0  12    2 9611009                               6 170 161   9   0  14    8 200 206                  15 143 162   L=1 386 333
 11 244 251   4  24  65   H,K= 3, 4     H,K= 5, 1     8   0  42  11 259 266   10 263 263     H,K= 16, 0   17 129 130    5 894 901
 13  46  35   6  39  41   L=0 100091040  L=010091040 10   0  35   13 118 128   L=1 289 271   L=0 393 376  19   0  70    714981449
 15   0  63   8 986 948    3 191 187     2 454 436   12 349 351   15  31  61    3 399 401                               9 565 589
 17   0  22  10 690 674    5 583 577     4 638 612   14 177 174                5  31  68     H,K= -1, 1   H,K= -2, 4   11  94 119
 19   0  58  12 952 893    4 136 404     6 104  91   16  46  49   H,K= 8, 4    7 141 117     L=2 879 856  L=2 510 538  13 337 363
             14 104 124    9  63  55     8 138 160                L=0  90  90                4 209 210    4 211 211   15  95 128
H,K= 0, 4    16 425 438   11 459 472    10 368 341   H,K= 6, 5    2 509 474   H,K= 11, 1     6 769 844    6 459 461   17 129 161
L=0  44  47  18  70  89   13 175 201    12 237 234   L=1 335 301  4 379 388   L=0   0  67    8 541 553    8 154 162   10 356 366
 2 278 280   20 328 283   15 223 236    14 235 242   3 117  81   6 124 150    2 473 468     10   0  45    12 230 252   19 161 166
 4 273 280   22   0  54   17   0  18    16 425 434   5 439 451   8 180 162    4   0   7     12 202 217   14 195 191
 6 502 495                               18 308 296   7 205 176  10  51  79    6 214 219     14 486 488   16 306 314   H,K= -4, 2
 8 376 352   H,K= 2, 1   H,K= 3, 5     20  79 104   9 129 113   12   0  30    8 159 144     16 180 168   18 189 168   L=215681566
 10 493 477  L=1 553 471  L=0 225 203                11 227 251  14   0  51   10 413 452     18   0   7                 4 642 660
 12   0  55   3 516 499    2 344 333    H,K= 5, 2   13 113 116                12   0  43     20   0  29    H,K= -2, 5    6 138 171
 14  49  90   5 682 665    4   0  39    L=1 450 408               H,K= 8, 5   14   0  45     22 122 114   L=1 255 266    8   0  22
 16 179 189   7 395 396    6 319 307    3  81  78    H,K= 6, 6   L=1   0   5                               3   0  68   10 218 242
 18 143 120   9 133 102    8   0  18     5   0  40   L=0 109 125  3   0  17   H,K= 11, 2    H,K= -1, 2    5 381 390   12 464 484
            11 596 580    10 216 221    7 519 474    2 244 246   5 441 410   L=1 345 355    L=2 517 512    7 773 784   14 196 210
H,K= 0, 5    13  74  39   12  90  80    9  83 109    4 106  99   7   0  18    3 200 224     3 830 789     9 124 103   16 138 130
L=1  51  44  15  46  79   14 301 286   11 374 388    6 170 149   9   0  75    5 282 296     5 821 855    11 404 420   18   0  87
 3 448 464   17 241 244   16   0  25    13 255 248   8   0  33  11   0   6    7 363 360     7 532 552    13   0  32   20 195 203
 5 200 198   19 253 260                 15 170 170                            9   0  53     9 910 938    15 141 131
 7 374 374   21 223 231   H,K= 3, 6    17 177 162   H,K= 6, 7   H,K= 8, 6   11 179 174     11 505 524                 H,K= -4, 3
 9 122 127              L=1 104  66    19 115 100   L=0 182 175  L=0  90  90  13   0  18     13 448 460                L=1 842 843
 11   0  11  H,K= 2, 2    3   0  44                  2   0  25                              15 484 475    H,K= -2, 6   3 418 410
 13 188 194  L=0 358 376  5 136 157    H,K= 5, 3    4 250 239   H,K= 9, 1   H,K= 11, 3    17 258 258    L=2 289 279    5   0  50
 15  95 109   2 266 244   7   0  22    L=0 455 487   6 253 247   L=0 266 237  L=0  69  96    19 172 162    4 168 148    7 234 214
              4 466 502   9 186 183    2   0  41    8 257 257   2 241 217    2 404 399     21   0  60     6 235 217    8 110 137
H,K= 0, 6    6 434 423   11   0  38    4 562 567   10  51  35   4   0  32    4  93  66                    8 140 133    9  35   5
L=0 255 262  8 578 568                 6 447 422   12  26   7   6   0  36    6   0  60     H,K= -1, 3   10 214 203   10   0  76
 2   0   9   10 271 247  H,K= 3, 7    8 196 206   14 251 254   8 127 141    8 179 172     L=2 500 503   12  31  90   13 186 205
 4 392 386   12 273 262  L=0  72  66  10 333 323   16 133 159  10  60  47   10   0  87     4 241 220                 15 246 248
 6 180 173   14 533 508   2 267 266   12   0  21  18  85  87  12 285 312   12 285 312     6 333 317    H,K= -2, 7   17 283 305
 8 379 380   16  97 103   4 207 204   14 305 311               10 374 398     8 127 141    L=1 138 170  19  95 103
 10 161 168  18   0  31   6   0  11   16 150 112   H,K= 7, 2   14 227 259                  10 374 398    3 118  79
 12   0  28  20   0   5                            L=1 106 104  14 344 340   H,K= 11, 4   12 216 230    5 246 227   H,K= -4, 4
            H,K= 2, 3   H,K= 4, 0   H,K= 5, 4   3 615 625   16 427 414   L=1 246 220    14   0  44     7  72  77   L=2 232 264
H,K= 0, 7   L=1 138 170  L=0 163 100  L=1   0  76  5 454 459   18 143 161   3 234 250     15 115 134                 4 260 292
L=1 145 145  3 182 163   2 866 861   3 227 217   7 406 395    20 195 185   5 180 143     18 143 161   H,K= -3, 1   6 228 243
 3 104 129   5 431 429   423202337   5 164 185   9 805 781                 7 203 198     9 404 407    L=113211327   8  74  68
 5 106 113   7   0  29   6   0  11   7 278 267  11 434 432   H,K= 9, 2                                 3 425 467   10   0  44
 7   0  33   9 250 230  8 773 745   9 280 255  13 134 143   L=1 133 118   H,K= 11, 5   H,K= -1, 4    5 404 382   12   0  40
             11 143 138  10 273 261  11 255 242  15 134 124   3 133 145   L=0   0  51   L=1 368 377    7 400 398   14  97 122
H,K= 0, 1   13 328 333  14 496 487  13 154 168  17 159 185    5 338 329   2   0  66     3   0  25     9 223 218   16   0  37
L=0 938 974  15 184 162  16 191 153  15   0  29               7   0  51               5 140 123    11 353 363   H,K= -4, 5
  212611201  17 423 413  18 141 171  17   0  47  H,K= 7, 3    9 147 142  11   0 142    7 704 704   13   0  20   L=1 315 335
 4  83 101   19  70  52  20 186 159              L=0 292 296  11   0 142  13 141 140     9 176 175   15 115 134    3   0  19
 6   0  14               H,K= 4, 1   H,K= 5, 5   2 161 158              15 290 315     11   0  15   17  62  77    5 530 537
 8 177 183  H,K= 2, 4   L=1 471 482  L=0  94  46   4 423 437  H,K= 9, 3              13 195 190    20  53  20    7 115  95
 10 384 370  L=0 125 128 31057 994   2 202 192   6 191 189   L=0 494 484  H,K= 11, 6  15 115 134              L=113211327
 12 576 558  2  56  38   4   0  33   4 101 104   8 587 575   2 170 156  L=0 177 173   17  62  77   H,K= -3, 2   9 434 475
 14   0  11   4   0  33   6 404 399   6 228 213  10 218 224   4 294 296   2 195 213               L=113211327  11 168 149
 16 149 158  6 404 399   7 567 581   8  65  33  12   0  21   6  72  90   4   0  71   H,K= -1, 5    3 425 467  13 131 108
 18 333 308  8 298 279   9  97  82  10  85  31  14 182 169   8 124 118   6 333 343   L=2 539 533    5 404 382  15   0  16
 20   0  31  10 313 308  11 188 194  12 335 363  16 175 181  10 203 215  8 124 118    4   0   5    7 400 398
 22 131 131  12  62  75  13 313 312  14 122  90               12   0   0              6 368 360    9 223 218   H,K= -4, 6
            14 232 200  15 299 282              H,K= 7, 4   14 173 157  H,K= 12, 0    8  39  54   11 353 363   L=2  83 107
H,K= 1, 2   16  81  54  17 340 349  H,K= 5, 6   L=1 615 602              L=0 177 173  10 298 293   13   0  20    4 200 202
L=1   0  34  18   0  71  19 136 143  L=1 257 263   3 267 267  H,K= 9, 4   2 195 213  12 177 187   15 115 113    6  95 100
 3 643 641              21  72  31   3 223 206   5 108  76   L=1  62  72   4   0  15  14  88  79  17 266 266    8 168 175
 5 973 920  H,K= 2, 5               5 349 343   7 168 172   3  39  26   6 333 343  16  46   7   19 289 287   10  94  89
 7 372 377  L=1 603 615  H,K= 4, 2   7 129 104   9 159 144   5 145 160              21   0  35   12 170 117
 9 858 815   3 493 469  L=0 117 113   9 127 124  11 225 201   7 125 138  H,K= 12, 1             H,K= -3, 3
 11 455 457   5 159 150  2 405 407  11 177 188  13   0  40   9 276 299  L=1 246 241  L=1  86 101  H,K= -3, 3
 13   0  76   7   0   5  4 730 720              15 156 153   11   0 111   2   0   5   L=2 189 179  L=2 189 179  H,K= -4, 7
 15 124 101   9   0  47  6 972 928  H,K= 5, 7                13   0  28   4 173 146   5 313 313   6 686 697   L=1 106 148
 17 175 155  11 528 519   8   0  32  L=0 170 177  H,K= 7, 5                6  72  67   7 203 199   8  90 115    3   0  72
 19 326 314  13  53  53  10 282 272   2   0  50  L=0 136 136  H,K= 9, 5   8 173 185  11   0  40  10 255 251    5 150 140
 21  31  54  15  78  97  12  24  48               2 157 154  L=0 124 101  10  99  92  13 159 175  12  78  76
            14  76  80  H,K= 6, 0   4 360 347   4   0  57              14   0  60
H,K= 1, 3  H,K= 2, 6  16  86  82  L=0 108 113   6   0  19   4   0  38  H,K= 12, 3  L=2  62  75  16 246 274
L=0 175 167  L=0 198 194  18 186 176   219151882   8 207 294   6  99 111  3 340 344   6  90 119   18 109 144
  212091204  2 108  81  20 329 323   4 754 722  10 108 127   8 166 205              20   0 102
 4 869 855   4   0  73              6 762 748  12   0   5   H,K= 10, 0  5 173 159
 6 457 436   6 131 110  H,K= 4, 3   8 161 137              L=0 484 683  7  76  82  H,K= -2, 0   H,K= -3, 4
 8 287 277  8   0  47  L=1 787 747  10 934 905  H,K= 7, 6   2 858 859   9   0  19  L=218512076  L=1 212 200
 10 668 650  10   0  75  3 315 334  12 523 539  L=1 188 174   4   0   9              3 351 379
 12 120 114  12 145 143  5  67  81  14 562 552  3 129 139                          4 184 144    5 289 296
 14  72  60
```

Table 3 (cont.)

FO	FC	FO	FC	FO	FC	FO	FC	FO	FC	FO	FC	FO	FC	FO	FC	FO	FC

[Dense multi-column structure-factor table of Fo and Fc values grouped by H,K rows]

are completely coplanar, whereas the remaining two cyclobutanes, 7–8–9–1, and 5–4–3–2, have a puckered configuration. This result added another datum to the controversial question of configurations of relatively unstrained cyclobutane rings. A partial list of observed cyclobutane configurations in various types of compounds is given in the earlier paper (Okaya & Bed-

104 105
O(3) 111 110 O(4)
108 6

O(1) 126° O(2)
114° 119°
C(3)

(a)

+0·054 −0·088
O(3) −0·003 O(4) +0·090
6 −0·052

O(1) +0·006 O(2) +0·006
−0·016
+0·004
3

(b)

Fig. 5. Configurations of the two derivative groups. (a) Bond angles. (b) Planarity of the groups. Deviations of atoms from the least-squares planes are shown. See Fig. 4 for bond distances.

O(2)
1.24
1.51
1.730
9
1.27
3 1.55 1.54 1.58
O(1) 1.57 8
1.730 4 1.56 1.58 1.56 1 1.725
1.54
7 1.745
1.56 1.55 2
1.71 3 1.52
5
1.54 6
1.723 1.38 1.40
Ö(3)
1.46 O(4) 1.44
1.50

Fig. 4. Bond distances in the molecule, in Å.

nowitz, 1967). The geometry of the two cyclopentane rings is shown in Figs. 6 and 7. For each group, the four atoms involved in other cyclobutane ring formations lie on a perfect plane out of which the apex, 6, projects by about 0·7 Å. As shown in Fig.6(b) the bond angles show tendencies similar to those in the pentacyclodecane system [Fig.3(c)] (Okaya & Bednowitz, 1967). The results well established that, for cyclopentane rings in such a condensed system, the least-constrained apex carbon atoms undergo the largest deviations from the normal valence angles. As discussed previously, one of the diagonals of the cage is an approximate mirror plane; the planarity of the diagonal is also studied and the results shown in Fig.7(b).

The carbon atoms in the cage structure can be divided into four groups; (a) the apex, 6; (b) the nearest neighbors of the apex, 5 and 7; (c) four next nearest neighbors involved in cyclopentanes, 1,2,4 and 8; and (d) 3 and 9 of the base edge. Fig. 8(a)–(d) shows bond angles outside the ring system classified into these four groups. One notices obvious systematic variations in the bond angles. Similar variations have been observed in the decane compound (Okaya & Bednowitz, 1967).

The shape and size of the carboxyl and ethylenedioxy groups, can be seen in Figs. 4, and 5(a) and (b). The ethylenedioxy group (on 6) is a puckered ring with the C(6)–O distances shorter than CH₂–O by about 0·05 Å. The ring makes an angle of 88° with the diagonal mirror plane of the cage. The carboxyl group has the usual configuration found when there is a dimer formation.

(a)

(a)

AVERAGE OF FOUR CYCLOPENTANE RINGS IN C₁₀Cl₁₁OSO₂Cl

(b)
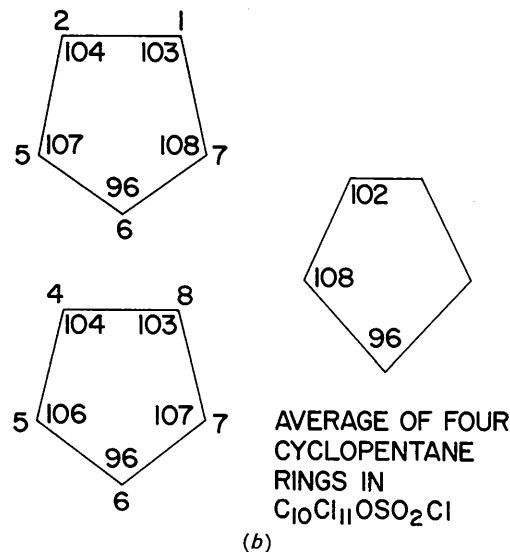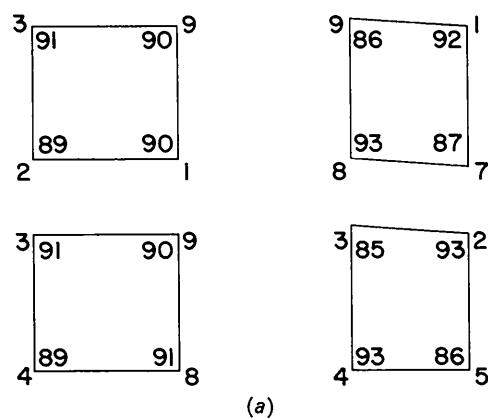
Fig.6. (a) Bond angles in the cyclobutane rings, in degrees. (b) Bond angles in the cyclopentane rings, in degrees. The average values of the four cyclopentanes in C₁₀Cl₁₁.OSO₂Cl, a pentacyclodecane compound, are shown for comparison. (Okaya & Bednowitz, 1967).

CYCLOPENTANES
C(6) NOT INCLUDED
IN EVALUATION

DIAGONAL PLANE

(b)
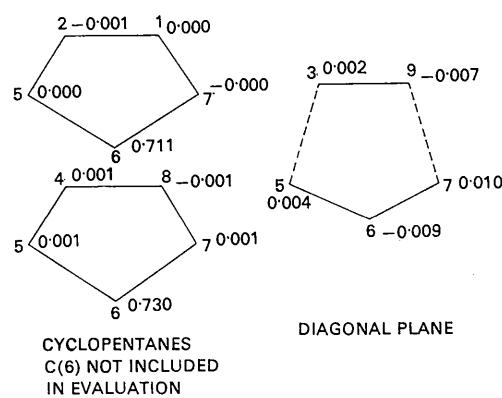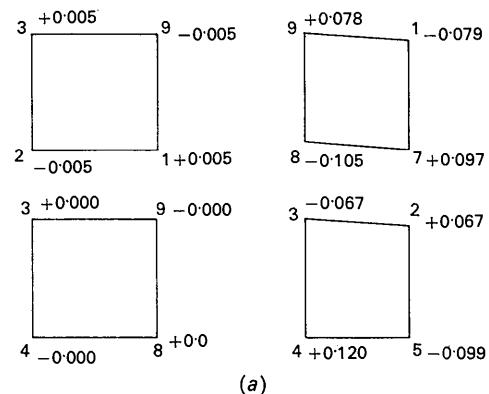
Fig. 7. (a) Planarity of the cyclobutane rings. The deviations of atoms from the least-squares planes are shown. The cyclobutanes are divided into two groups, coplanar and puckered (see text). (b) The planarity of the cyclopentanes and the diagonal plane. In evaluating the least-squares planes for the cyclopentanes, the apex carbon atom was not included. From the plane of the diagonal (which included the apex, 6), other carbons in the cage are shifted by the following amounts (in Å): C(1), 1·07; C(8), −1·07; C(2), 1·07; C(4), −1·06.

The crystal structure is a usual carboxyl acid structure. The carboxyl groups are involved in forming dimers around centers of symmetry by O–H··O hydrogen bonds of 2·60 Å and the dimeric molecules thus formed stack in the structure by usual van der Waals contacts. All intermolecular approaches exhibit normal separations. The general feature of the structure can be obtained from Fig. 2.

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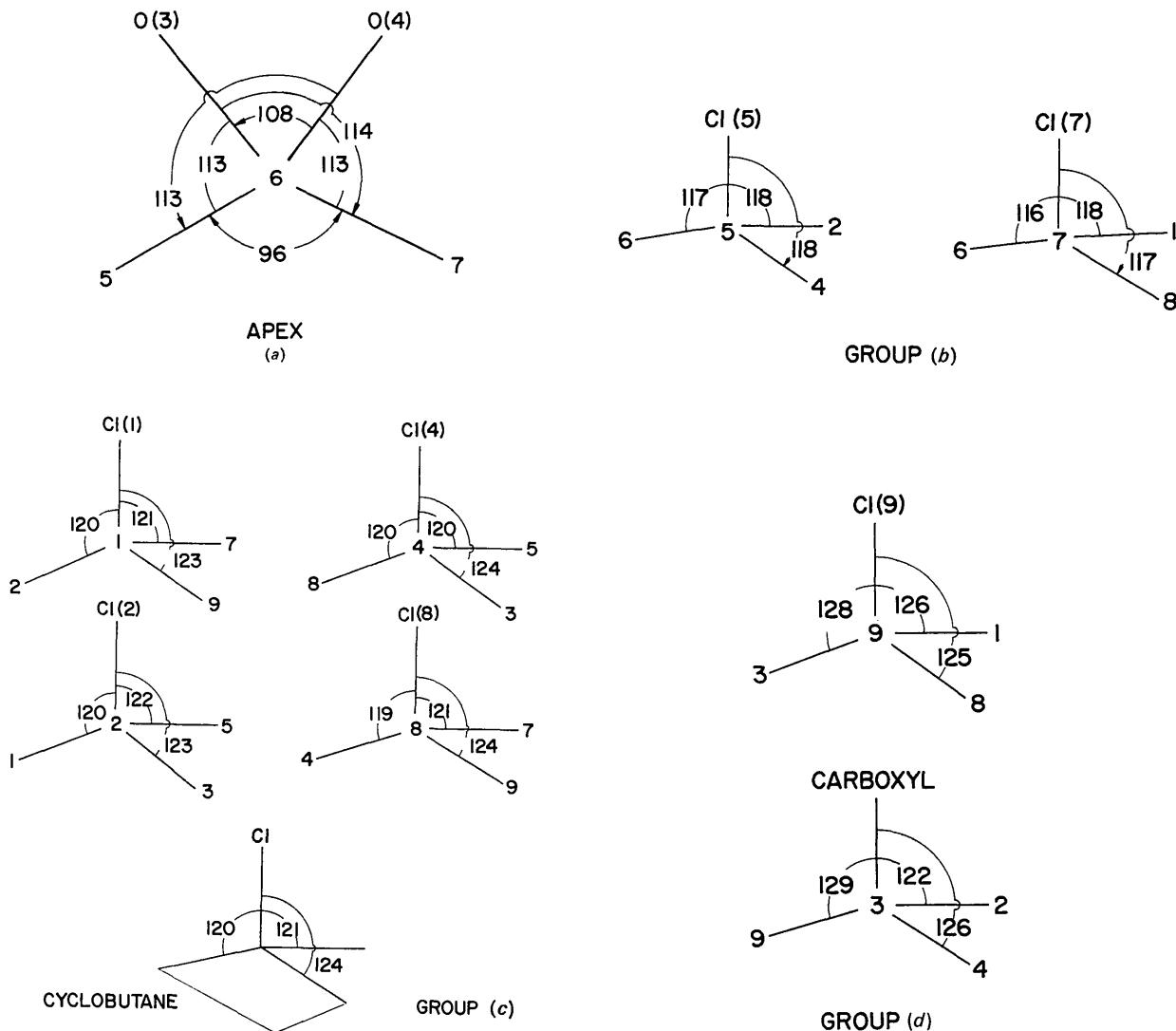
Fig. 8. Bond angles outside the cage skeleton, in degrees. (*a*) The apex carbon, 6. (*b*) Group *b*. (*c*) Group *c*. The average values for the four atoms are also shown. (*d*) Group *d*. For the four groups into which the skeleton carbon atoms are classified, see text.